Very Fast Field Oriented Control for Permanent Magnet Hysteresis Synchronous Motor

H. Lesani*, A. Darabi**, Z. Nasiri Gheidari*** and F. Tootoonchian****

Abstract: In this paper, a new field oriented control scheme with maximum torque for permanent magnet hysteresis synchronous (PMHS) motor has been presented. Vector control method provides significant improvement to the dynamic performance of ac motors but in this method d- axis current is controlled such as the ratio of motor torque to motor current is a maximum, then the dynamic performance will be very fast. Furthermore, d and q axis currents are limited such as stator winding currents remain in the allowed range. Feedback method is used for the decoupling the torque-current component from the flux-current component so these two components can be independently controlled. Simulation results for the motor are given and test results validate the theoretical performances.

Keywords: Permanent Magnet Hyateresis Motor (PMHS), Field Oriented Control, Decoupling Method, Torque per Ampere

1 Introduction

Hysteresis synchronous motor is widely used in small motor applications. It has some advantages such as constant torque during the run-up period, and it can pull into synchronism any load inertia that it can accelerate. Its starting current is usually less than 180% of the full-load current [1].

The combination of permanent magnet and hysteresis materials in the rotor of the hybrid motor has many distinct advantages over the conventional PM or hysteresis motors [2], [3]. The hybrid motor in which the permanent magnets are inserted into the slots at the inner surface of the hysteresis ring is called the permanent magnet hysteresis synchronous (PMHS) motor [4]. During asynchronous speed, the motor torque consists of the hysteresis torque, eddy current torque and permanent magnet brake torque. At synchronous speed the motor torque comprises of the hysteresis and combines magnet torques. It permanent the advantageous features of both the hysteresis and

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permanent magnet motors. The negative affect of the magnet brake torque is compensated by the eddy current torque, particularly at the initial run up period [5].

In motor drive technology, dc motors are still widely used in many applications which require precise speed control and fast dynamic response [6]. Since the dc motor has many drawbacks, such as high cost of maintenance, the use of the ac motor instead of the dc motor in adjustable speed drive system has received wide attention [7]. The field oriented control scheme [8, 9] is widely used to improve the performance of the ac motor in such a system. Using the field oriented control, the performance of the ac motor can be greatly enhanced [10, 11].

The detailed derivation of the PMHS motor torque equation and the design of the digital speed controller for the DSP based PMHS motor vector control system is reported in [12]. But it hasn't any decoupling technique and the d-axis stator current i_{ds} , set to zero. An analysis and microprocessor implementation of the field oriented control scheme for a laboratory prototype PMHS motor are presented in [7] also. Reference [7] decoupled the variables of δ and stator currents i_{ds} and i_{qs} by rotating the stator frame to align to the rotor frame and it also used $i^{(r)}_{ds}=0$. Finally PWM vector control simulation results for the motor drives are given in [13] as a section of paper, very briefly.

The objective of this paper is to present a mathematical model of the poly phase PMHS motors and vector control of them. Stator d-axis current is controlled such as the ratio of motor torque to motor current is a maximum, then the dynamic performance will be faster. Furthermore, this current is limited such as stator

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winding currents remain in the allowed range. Feedback method is used for the decoupling the torque-current component from the flux-current component, so these two components can be independently controlled. Finally simulation results are compared with experimental ones of [6] that show good agreement.

2 Motor Model

The following assumptions are considered in the analysis.

a) The stator is assumed to have a sinusoidally distributed polyphase windings [4].

b) The magnetic flux is radial in the air gap and circumferential in the rotor hysteresis material [4].

c) The hysteresis effects in the rotor hysteresis materials are taken into account in the case of both running up and synchronizing operation [5].

d) The effects of saturations is neglected [5].

e) The B-H loop of the hysteresis material is modeled by a parallelogram [5].

Figure 1 shows the model of a three phase PMHS motor. Each stator winding has a leakage flux and a main flux that links the rotor. The hysteresis phenomenon in an element of the rotor ring is represented by a balanced polyphase winding, and therefore by two orthogonal closed coils, each with the same number of turns as the stator coil pair.

The stator variables are transformed to the rotor reference frame which eliminates the time-varying inductances in the voltage equations. Park's equations are obtained by setting the speed of the stator frame equal to the rotor speed. The voltage-current equations are as shown in Eq. (1).

$$\begin{bmatrix} V_{ds} & V_{qs} & V_{dr} & V_{qr} & V_{pm} \end{bmatrix}^{t} = \begin{bmatrix} R_{s} + \frac{p}{\omega_{b}} X_{ss} & -\frac{\omega_{r}}{\omega_{b}} X_{ss} & \frac{p}{\omega_{b}} X_{m} & -\frac{\omega_{r}}{\omega_{b}} X_{m} & \frac{p}{\omega_{b}} X_{m} \\ \frac{\omega_{r}}{\omega_{b}} X_{ss} & R_{s} + \frac{p}{\omega_{b}} X_{ss} & \frac{\omega_{r}}{\omega_{b}} X_{m} & \frac{p}{\omega_{b}} X_{m} & \frac{\omega_{r}}{\omega_{b}} X_{m} \\ \frac{p}{\omega_{b}} X_{ss} & 0 & R_{r} + \frac{p}{\omega_{b}} X_{rr} & 0 & \frac{p}{\omega_{b}} X_{m} \\ 0 & \frac{p}{\omega_{b}} X_{m} & 0 & R_{r} + \frac{p}{\omega_{b}} X_{rr} & 0 \\ \frac{p}{\omega_{b}} X_{m} & 0 & \frac{p}{\omega_{b}} X_{m} \end{bmatrix}$$
(1)
$$\times \begin{bmatrix} i_{ds} & i_{dr} & i_{dr} & i_{dr} \end{bmatrix}^{t}$$

The electromagnetic developed torque in a three-phase, P pole motor is given by [13]:

$$T_{e} = \frac{3}{2} P[(L_{ds} - L_{qs})i_{ds}i_{qs} + L_{md}i_{dr}i_{qs} - L_{mq}i_{qr}i_{ds}]$$
(2)

where V_{ds} , V_{qs} are d, q axis stator voltages, V_{dr} , V_{qr} are d, q axis rotor voltages, i_{ds} , i_{qs} are d, q axis stator currents, i_{dr} , i_{qr} are d, q axis rotor currents, R_s , X_{ss} are

resistance and reactance of stator circuit, R_r , X_{rr} are resistance and reactance of rotor circuit, L_{md} , L_{mq} are dq axis mutual inductance between rotor and stator circuits, L_{ds} , L_{qs} are d-q axis inductance of stator, ω_b is base angular frequency, ω_r is rotor angular frequency, T_L is load torque, H is inertia constant, p is d/dt and P is number of pole pairs.

The electrical equivalent circuits of the hysteresis synchronous motor are presented in [13]. The motor has a standard three-phase, four-pole stator winding. Its ratings are 208 V, 5 hp and 60 Hz. Pertinent design dimensions, the rotor hysteresis material and motor equivalent circuit parameters are given in [1].

The state equations on the rotating dq0 reference frame are introduced by considering:

Input Vector =
$$[V_{ds}, V_{qs}, V_{dr}, V_{qr}, T_L]$$

Output Vector = $[i_{ds}, i_{qs}, i_{dr}, i_{qr}, T_e, \omega_r]$ (3)
State Variable = $[\psi_{ds}, \psi_{qs}, \psi_{dr}, \psi_{dr}]$

MATLAB and Simulink softwares are used for simulation propose.

3 Torque Expression

Torque expression for PMHS motor is given in Eq. (2). In the next step d-axis current should be calculated for torque-per-ampere current control that minimizes the copper loss.

Q-axis current can be written as a function of nominal stator current amplitude and d-axis current, as shown in Eq. (4).

$$i_{ds}^{2} + i_{qs}^{2} = |\dot{i}_{s}|^{2} \implies i_{qs}^{2} = |\dot{i}_{s}|^{2} - i_{ds}^{2}$$
 (4)

Substituting Eq. (4) in Eq. (2) and after some algebraic operations, the Electromagnetic torque given by:

$$T_{e} = \frac{3}{2} P[(L_{ds} - L_{qs})i_{ds}\sqrt{|i_{s}|^{2} - i_{ds}^{2}} + L_{md}i_{dr}\sqrt{|i_{s}|^{2} - i_{ds}^{2}} - L_{mq}i_{qr}i_{ds}]$$
(5)

 i_{dr} , i_{qr} and nominal stator current magnitude (|is|) are constant [7], [14]. So:

$$\frac{\partial T_{e}}{\partial i_{ds}} = 0 \qquad \Rightarrow \qquad i_{ds} = \frac{L_{md}i_{dr} \pm \sqrt{a}}{4(L_{ds} - L_{qs})}$$
(6)

where:

$$a = (L_{md}i_{dr})^{2} + 8(L_{ds} - L_{qs})^{2} |\dot{i}_{s}|^{2} - 8L_{mq}(L_{ds} - L_{qs})\dot{i}_{qr}$$
(7)

On the other hand, calculated i_{ds} may be result the stator winding current rise from allowed range, so it should be limited. So, stator current is compared with allowed range (3 times of rating current usually) and when it was increased, i_{ds} will be limited.

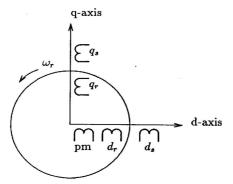


Fig. 1 d-q Axis model of PMHS motor.

4 Results And Discussions

Complete control schematic is shown in Fig. 2. First, the phase currents are transformed to a space vector in stator–coordinates, and secondly, this space vector is transformed to a d–q axis in the rotor frame. The stator-to-rotor transformation depends on the actual rotor position. Therefore, the rotor position must be determined during every sampling cycle.

The drive is fed in such a way that the q-axis current provides the desired torque. Since the d-axis of the current vector points to the magnetization direction of the rotor pole, the d-axis current is suppressed by the corresponding controller. The drive consists of three controllers, namely, the d-axis controller, the q-axis controller, and the speed controller [13].

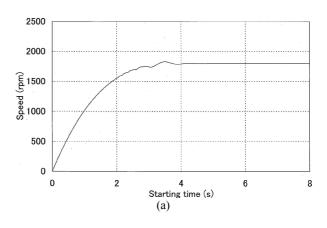
D-axis current reference comes from torque-per-ampere calculation block and limitation block limit the i_{ds} such as stator winding current is remain in allowed range.

Figure 3 shows the test and computed open loop speedversus-time. Figure 3(a) and (b) shows the computed and experimental speed-versus-time responses of PMHS motor from [4] and (c) shows simulation result of [5]. It is seen that the computed speed response is smoother than the experimental result. The reason is due to the difference between the cataloged and calculated areas of the hysteresis B-H loop. Because of this, it is considered that the hysteresis torque component of the computed torque is larger than the experimental result so that the computed time to reach at synchronous speed is shorter than the experimental one. The measured starting time is approximately 5.0 s and the computed time is about 4 s for [4] and 3.8 s for [5]. But all of these responses are open loop.

Vector control method provides significant improvement to the dynamic performance of ac motors but in proposed method d- axis current is controlled such as the ratio of motor torque to motor current is a maximum, then the dynamic performance will be very fast. It is shown in Fig. 4. Continues line is related to conventional control method and dash line is to proposed method. Starting time is approximately 0.9 sec. for conventional and about 0.45 sec. for proposed method.

Comparison between open loop and closed loop control result shows the advantages of vector control method.

The experimental speed responses of the field oriented control to a step load change at 40 Hz and 70 Hz are shown in the curves of Figs. 5(a) and 6(a), respectively from [6] and proposed method results are shown in 5(c) and 6(c). It was observed that the PMHS motor can operate smoothly in response to the step load change.



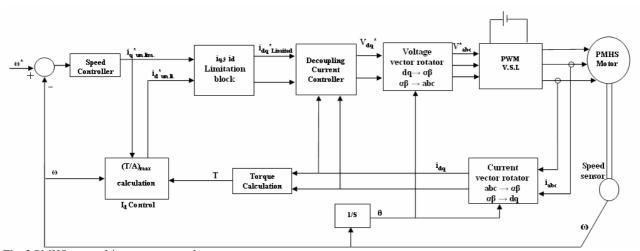


Fig. 2 PMHS motor drive vector control structure.

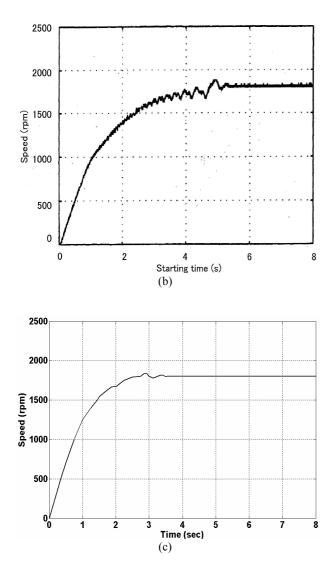


Fig. 3 Open Loop speed–time response. (a) Computed speed–time response [4]. (b) Test speed–time response [4]. (c) Computed speed–time response with presented method.

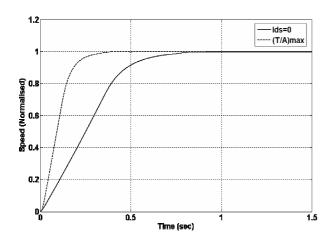


Fig. 4 Closed loop control speed–time response. Continues line is related to conventional control method and dash line is to proposed method.

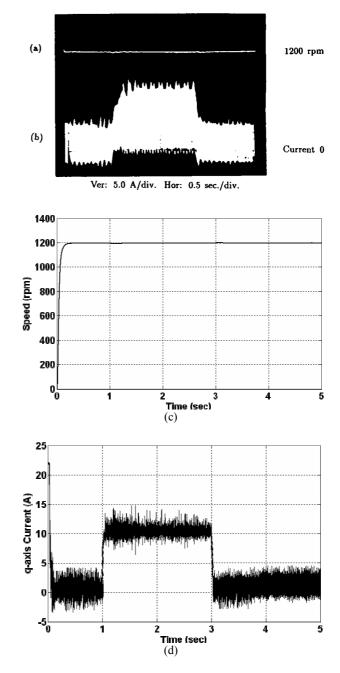
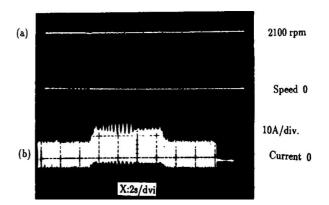


Fig. 5 Speed and dc link current responses to step load at 40 Hz. (a) conventional control speed at 1200 rpm [6] (b) conventional control dc current [6] (c) proposed control speed (d) proposed control dc current.



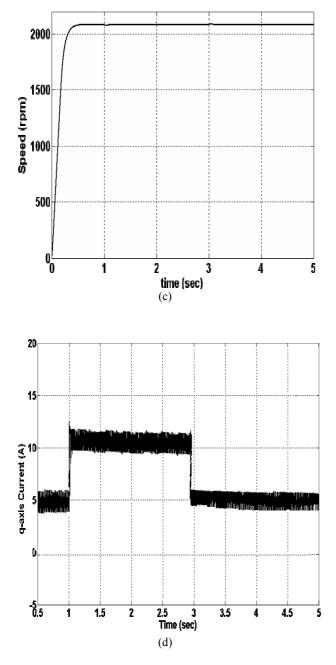


Fig. 6 Speed and dc link current responses to step load at 70 Hz. (a) Conventional control speed at 2100 rpm [6] (b) conventional control dc current [6] (c) proposed control speed (d) proposed control current.



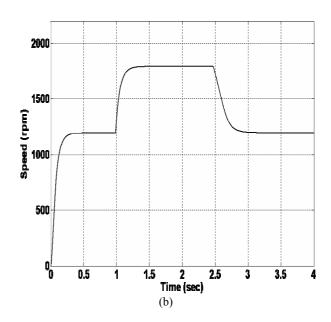


Fig. 7 speed curve of motor at frequency of 40-70-40 Hz (a) conventional control speed curve [6] (b) proposed control speed curve

Figures 5(b) and 6(b) show the experimental dc link current responses at the sudden load change test from [6] and Figs. 6(d) and 7(d) shows simulation results. It can be seen from Figs. 5(b,d) and 6(b,d) that the dc link current increased from no load to full load in about 0.25 second in conventional control method and less than 0.05 second in proposed method, which reflects a quick response of the field oriented control system to the sudden load changes.

The speed of the PMHS motor is presented in Fig. 7. The test was conducted by step frequency change from 40 Hz to 70 Hz and then returning to 40 Hz. Figure 7(a) shows the test results from [6] and Fig. 7(b) shows the proposed method result.

It can be seen from Fig. 7 the proposed method has a very fast response for step change in reference speed. Speed in conventional control increased from 1200 rpm to 2100 rpm in about 4 second [6] and approximately 0.4 second in proposed method, which reflects a quick response of the proposed control system to the sudden speed changes.

When the frequency command was changed from 70 Hz to 40 Hz, the speed response was found to be much fast in conventional control. The transient period was less than 1 second for conventional control [6] and about 0.4 second for proposed method. The response of proposed method is very faster in both acceleration and deceleration.

This asymmetrical characteristic during the acceleration and deceleration of the PMHS motor may explain that there was a brake torque due to the permanent magnets [6].

5 Conclusion

An analytical model for a permanent magnet hysteresis hybrid synchronous motor has been developed. A field oriented control scheme has been successfully simulated and a new strategy for calculating d-axis current for maximum torque-per-amper is proposed. Furthermore d-axis current is limited such as the stator winding current remains in allowed range.

This method causes to very fast dynamic performance of motor. Comparison between test and simulation results show the proposed method is sufficient. The simulation results have faster response and confirm the improvement of the dynamic performances using a field-oriented control with maximum torque-per-amper strategy.

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